## Package 'gretel'

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Title Generalized Path Analysis for Social Networks

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Description The social network literature features numerous methods for assigning value to paths as a function of their ties. 'gretel' systemizes these approaches, casting them as instances of a generalized path value function indexed by a penalty parameter. The package also calculates probabilistic path value and identifies optimal paths in either value framework. Finally, proximity matrices can be generated in these frameworks that capture high-order connections overlooked in primitive adjacency sociomatrices. Novel methods are described in Buch (2019) <https: //davidbuch.github.io/analyzing-networks-with-gretel.html>. More traditional methods are also implemented, as described in Yang, Knoke (2001) <doi:10.1016/S0378-8733(01)00043-0>.

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URL https://github.com/davidbuch/gretel

BugReports https://github.com/davidbuch/gretel/issues License GPL-3 Depends R (>= 3.0) Imports Rcpp (>= 1.0.0), ResistorArray (>= 1.0-32) LinkingTo Rcpp Suggests knitr, rmarkdown, testthat (>= 2.1.0) VignetteBuilder knitr LazyData true RoxygenNote 6.1.1 NeedsCompilation yes Author David Buch [aut, cre] (<https://orcid.org/0000-0002-4574-0075>) Repository CRAN Date/Publication 2019-08-22 12:00:02 UTC

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all\_opt\_gpv Optimize All Generalized Path Values

#### Description

Identify the path of optimal generalized path value from every source to every target in sociomatrix.

#### Usage

all\_opt\_gpv(sociomatrix, p = Inf, node\_costs = NULL)

## Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
р	a nonnegative real number that sets the 'p-norm' parameter for generalized path value calculation.
node_costs	a list of costs, in order, of all nodes represented in the sociomatrix, all are assumed 0 if unspecified

## Value

All optimal paths from source to target nodes in sociomatrix. To minimize memory usage, paths are returned as a list of trees in Dijkstra's format. Specific paths can be unpacked with unpack as described in the example below.

#### all\_opt\_ppv

#### See Also

gpv to calculate the value of a user-specified path,  $opt_gpv$  to identify the optimal path from a single source node to a single target node

all\_opt\_ppv

Optimize All Probabilistic Path Values

#### Description

Identify the path of optimal probabilistic path value from every source to every target in sociomatrix.

#### Usage

```
all_opt_ppv(sociomatrix, odds_scale = 1, odds_scale_by_node = NULL)
```

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
odds_scale	a nonnegative real number indicating the observed tie strength value that corre-
	sponds to 1-1 transmission odds
odds_scale_by_node	

sets a transfer odds scale for each node in a probabilistic path value calculation.

#### Value

All optimal paths from source to target nodes in sociomatrix. To minimize memory usage, paths are returned as a list of trees in Dijkstra's format. Specific paths can be unpacked with unpack as described in the example below.

#### See Also

ppv to calculate the value of a user-specified path, opt\_ppv to identify the optimal path from a single source node to a single target node

binary_distance	Binary Distance of a Network Path
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#### Description

Calculates the binary distance of a user-specified network path through a network, if all edges exist. Otherwise, returns Inf to signify infinite distance.

#### Usage

```
binary_distance(sociomatrix, path)
```

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
path	an integer vector of node indices from sociomatrix.

## Examples

```
## Calculate binary distance along a path in a sociomatrix
binary_distance(YangKnoke01, path = c(1,2,5))
```

```
## This path doesn't exist
binary_distance(YangKnoke01, path = c(1,2,4,5))
```

BuchDarrah19 Example data for gretel

## Description

A sociomatrix encoding tie strengths among five nodes

## Usage

BuchDarrah19

#### Format

a numeric matrix with 5 rows and 5 columns

#### Source

<DOI:10.1016/j.socnet.2010.03.006>

dijkstra\_inf Find the shortest L-Inf norm paths to other vertices

## Description

Find the shortest L-Inf norm paths to other vertices

#### Usage

dijkstra\_inf(dist, src)

#### Arguments

dist	A matrix of distances between nodes
src	An integer vertex ID

#### dijkstra\_nodes

#### Value

A numeric vector, entry *i* of which is the vertex immediately preceeding vertex *i* in the shortest path leading to *i*. Full paths must be constructed recursively.

dijkstra\_nodes Find the shortest paths to other vertices

#### Description

Find the shortest paths to other vertices

#### Usage

dijkstra\_nodes(dist, src, node\_costs)

#### Arguments

dist	A matrix of distances between nodes
src	An integer vertex ID
node_costs	a list of costs, in order, of all nodes represented in the sociomatrix, all are assumed 0 if unspecified

#### Value

A numeric vector, entry *i* of which is the vertex immediately preceeding vertex *i* in the shortest path leading to *i*. Full paths must be constructed recursively.

flament\_average\_path\_length

Yang and Knoke's Average Path Length

## Description

Calculates 'APL' (Average Path Length) as defined in Yang, Knoke (2001). Called flament\_average\_path\_length in homage to A.C. Flament, who defined path length in 1963.

#### Usage

flament\_average\_path\_length(sociomatrix, path)

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
path	an integer vector of node indices from sociomatrix.

#### See Also

flament\_path\_length

#### Examples

```
## Calculate 'APL' of a path in a sociomatrix
flament_average_path_length(YangKnoke01, path = c(1,2,5))
```

```
## This path doesn't exist
flament_average_path_length(YangKnoke01, path = c(1,2,4,5))
```

flament\_path\_length Flament's Path Length Measure

#### Description

Calculates path length as defined in Flament (1963). That is, sums the values of each edge in the path, if all edges exist. Otherwise, returns NA.

#### Usage

flament\_path\_length(sociomatrix, path)

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
path	an integer vector of node indices from sociomatrix.

#### See Also

flament\_average\_path\_length

## Examples

```
## Calculate Flament's Path Length along a path in a sociomatrix
flament_path_length(YangKnoke01, path = c(1,2,5))
```

```
## This path doesn't exist
flament_path_length(YangKnoke01, path = c(1,2,4,5))
```

generate\_proximities Generate a Proximity Matrix

#### Description

Generates a proximity matrix in one of three modes:

- 'ogpv' Optimal Generalized Path Value. Entry i, j of the proximity matrix will equal the optimal 'gpv' among all paths connecting node i to node j.
- 'oppv' Optimal Probabilistic Path Value. Entry i, j of the proximity matrix will equal the optimal 'ppv' among all paths connecting node i to node j.
- 'sconductivity' Social Conductivity (Random Walk Probability). If each tie strength recorded in sociomatrix is taken to be analogous to the conductivity of an electrical component, i, j of the proximity matrix will equal total conductivity of all paths from node i to node j.

#### Usage

```
generate_proximities(sociomatrix, mode = c("ogpv", "oppv",
    "sconductivity"), p = Inf, node_costs = NULL, odds_scale = 1,
    odds_scale_by_node = NULL)
```

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.	
mode	a selection of 'ogpv', 'oppv', or 'sconductivity'	
р	if mode is 'ogpv', determines 'p-norm' parameter for generalized path value calculation.	
node_costs	if mode is 'ogpv', assigns transmission costs to vertices within the sociomatrix.	
odds_scale	if mode is 'oppv', sets a global transfer odds scale for probabilistic path value calculation.	
odds_scale_by_node		
	if mode is 'oppv', sets a transfer odds scale for each node in a probabilistic path value calculation.	

#### See Also

gpv, ppv

#### Examples

```
## Generate a proximity matrix in each mode
## Optimal Generalized Path Value
generate_proximities(YangKnoke01, mode = "ogpv", p = Inf, node_costs = c(1,3,3,2,1))
## Optimal Probabilistic Path Value
generate_proximities(YangKnoke01, mode = "oppv", odds_scale = 2)
```

```
## Sconductivity
generate_proximities(YangKnoke01, mode = "sconductivity")
```

gpv

#### Generalized Path Value

#### Description

Calculates the generalized path value of a user-specified path through sociomatrix. Parameter p sets the p-norm used in calculation.

#### Usage

gpv(sociomatrix, path, p = Inf, node\_costs = NULL)

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
path	an integer vector of node indices from sociomatrix.
р	a nonnegative real number that sets the 'p-norm' parameter for generalized path value calculation.
node_costs	a list of costs, in order, of all nodes represented in the sociomatrix, all are assumed 0 if unspecified

#### Details

As a rule of thumb, p close to 0 will downweight the impact of particular tie strengths and upweight the impact of binary path length. p equal to infinity will recapitulate the traditional path value measure of Peay (1980) and is therefore the default. In other words, the value of a path under p = Inf will be the value of the weakest tie. The value of the same path under p = 0 will be the inverse of its binary length.

#### See Also

opt\_gpv to identify the path of optimal 'gpv' between two nodes and all\_opt\_gpv to identify the optimal paths between all pairs of nodes. Calling generate\_proximities with mode = 'gpv' returns a matrix 'gpv' values for the optimal paths between all pairs of nodes.

#### Examples

## Calculate gpv along a path in a sociomatrix
gpv(YangKnoke01, path = c(1,2,5), p = 1)
## The same calculation, with nonzero node costs
gpv(YangKnoke01, path = c(1,2,5), p = 1, node\_costs = c(1,3,3,2,1))

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#### gretel

```
## This path doesn't exist
gpv(YangKnoke01, path = c(1,2,4,5), p = 0)
```

gretel

sconduct: Generalized Path Analysis for Social Networks

#### Description

This package contains two categories of functions. The first category is concerned with assigning values to user specified paths, while the second identifies paths of optimal value.

#### Details

Key functions in the path value calculation category are - gpv, which calculates Generalized Path Value - ppv, which calculates Probabilistic Path Value - binary\_distance, peay\_path\_value, flament\_path\_length, peay\_average\_path\_value, and flament\_average\_path\_length, which calculate path value measures described in *Yang, Knoke* (2001). - generate\_proximities, which generates a matrix of values representing the measures of optimal paths from each source node (row index) to each target node (column index).

Key functions in the optimal path identification category are - opt\_gpv, which identifies the path of optimal Generalized Path Value from a particular source node to a particular target node - opt\_ppv, which identifies the path of optimal Probabilistic Path Value from a particular source node to a particular source node to a particular target node - all\_opt\_gpv, which identifies the 'gpv'-optimal paths from every source node to every target node - all\_opt\_ppv, which identifies the 'ppv'-optimal paths from every source node to every target node - unpack, which unpacks the Dijkstra-format encoded shortest paths returned by all\_opt\_gpv and all\_opt\_ppv. See their help pages for details.

OpsahlEtAl10

Example data from Opsahl, Agneessens, Skvoretz (2010)

#### Description

A sociomatrix encoding tie strengths among five nodes, used for examples in Opsahl, Agneessens, Skvoretz (2010) Social Networks 32(2010):245-251

#### Usage

OpsahlEtAl10

#### Format

a numeric matrix with 5 rows and 5 columns

#### Source

<DOI:10.1016/j.socnet.2010.03.006>

opt\_gpv

#### Description

Identify the path of optimal generalized path value from a source node to a target node.

## Usage

```
opt_gpv(sociomatrix, source, target, p = Inf, node_costs = NULL)
```

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
source	an integer index corresponding to a node in sociomatrix
target	an integer index corresponding to a node in sociomatrix
р	a nonnegative real number that sets the 'p-norm' parameter for generalized path value calculation.
node_costs	a list of costs, in order, of all nodes represented in the sociomatrix, all are as- sumed 0 if unspecified

## See Also

gpv to calculate the value of a user-specified path, all\_opt\_gpv to simultaneously identify the optimal paths from any source node to any target node.

opt_ppv	Optimize Probabilistic Path Value	
opt_ppv	Optimize Probabilistic Path Value	

## Description

Identify the path of optimal probabilistic path value from a source node to a target node.

#### Usage

## Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
source	an integer index corresponding to a node in sociomatrix
target	an integer index corresponding to a node in sociomatrix
odds_scale	a nonnegative real number indicating the observed tie strength value that corre-
	sponds to 1-1 transmission odds
odds_scale_by_node	
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sets a transfer odds scale for each node in a probabilistic path value calculation.

#### See Also

ppv to calculate the value of a user-specified path, all\_opt\_ppv to simultaneously identify the optimal paths from any source node to any target node.

#### peay\_average\_path\_value

Yang and Knoke's Average Path Value

#### Description

Calculates 'APV' (Average Path Value) as defined in Yang, Knoke (2001) Called peay\_average\_path\_value in homage to E.R. Peay, who defined path length in 1980.

## Usage

```
peay_average_path_value(sociomatrix, path)
```

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
path	an integer vector of node indices from sociomatrix.

#### See Also

peay\_path\_value

#### Examples

```
## Calculate 'APV' of a path in a sociomatrix
peay_average_path_value(YangKnoke01, path = c(1,2,5))
```

```
## This path doesn't exist
peay_average_path_value(YangKnoke01, path = c(1,2,4,5))
```

peay\_path\_value Peay's Path Value Measure

#### Description

Calculates path value as defined in Peay (1980). That is, returns the value of the weakest connection in the path, if all edges exist. Otherwise, returns 0.

#### Usage

```
peay_path_value(sociomatrix, path)
```

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.
path	an integer vector of node indices from sociomatrix.

## See Also

peay\_average\_path\_value

#### Examples

## Calculate Peay's Path Value along a path in a sociomatrix
peay\_path\_value(YangKnoke01, path = c(1,2,5))

## This path doesn't exist
peay\_path\_value(YangKnoke01, path = c(1,2,4,5))

ppv

Calculate probabilistic path value

#### Description

Given a real valued sociomatrix, a path, and an optional odds\_scale, ppv calculates the transmission odds for the path and returns the transmission odds times odds\_scale so the result can be directly compared with observed tie strenghts.

#### Usage

```
ppv(sociomatrix, path, odds_scale = 1, odds_scale_by_node = NULL)
```

#### Arguments

sociomatrix	a nonnegative, real valued sociomatrix.	
path	an integer vector of node indices from sociomatrix.	
odds_scale	a nonnegative real number indicating the observed tie strength value that corresponds to 1-1 transmission odds	
odds_scale_by_node		
	sets a transfer odds scale for each node in a probabilistic path value calculation.	

## Details

We assume that observed tie strengths in sociomatrix are linearly proportional to transmission odds. That is, if the transmission odds for a strength 1 tie are 1 to 1, the transmission odds for a strength 5 tie are 1 to 5.

#### unpack

#### See Also

opt\_ppv to identify the path of optimal 'ppv' between two nodes and all\_opt\_ppv to identify the optimal paths between all pairs of nodes. Calling generate\_proximities with mode = 'ppv' returns a matrix 'ppv' values for the optimal paths between all pairs of nodes.

#### Examples

```
## Calculate ppv along a path in a sociomatrix
ppv(YangKnoke01, path = c(1,2,5), odds_scale = 3)
```

```
## This path doesn't exist
gpv(YangKnoke01, path = c(1,2,4,5))
```

unpack

Unpacks a Path from a Dijkstra-Format Spanning Tree

#### Description

Used with all\_opt\_gpv and all\_opt\_ppv to unpack individual paths from the Dijkstra-format trees that those functions return.

#### Usage

```
unpack(tree, source, target)
```

#### Arguments

tree	a Dijkstra-format tree returned by all_opt_gpv or all_opt_ppv
source	an integer index corresponding to a node in sociomatrix
target	an integer index corresponding to a node in sociomatrix

#### Details

Returns NA if a path does not exist

YangKnoke01

## Description

A sociomatrix encoding tie strengths among five nodes, used for examples in Yang, S., Knoke, D. (2001) Social Networks 23(4):285-295

#### Usage

YangKnoke01

#### Format

a numeric matrix with 5 rows and 5 columns

## Source

<DOI: 10.1016/S0378-8733(01)00043-0>

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