Package 'BayesNSGP'

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Title Bayesian Analysis of Non-Stationary Gaussian Process Models

Description Enables off-the-shelf functionality for fully Bayesian, nonstationary Gaussian process modeling. The approach to nonstationary modeling involves a closed-form, convolution-based covariance function with spatially-varying parameters; these parameter processes can be specified either deterministically (using covariates or basis functions) or stochastically (using approximate Gaussian processes). Stationary Gaussian processes are a special case of our methodology, and we furthermore implement approximate Gaussian process inference to account for very large spatial data sets (Finley, et al (2017) arXiv:1702.00434v2). Bayesian inference is carried out us-

ing Markov chain Monte Carlo methods via the 'nimble' package, and posterior predic-

tion for the Gaussian process at unobserved locations is provided as a post-processing step.

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calcQF

Calculate the Gaussian quadratic form for the NNGP approximation

Description

calcQF calculates the quadratic form in the multivariate Gaussian based on the NNGP approximation, for a specific parameter combination. The quadratic form is $t(u)C^{-1}v$.

Usage

calcQF(u, v, AD, nID)

u	Vector; left product.
V	Vector; right product
AD	N x (k+1) matrix; the first k columns are the 'A' matrix, and the last column is the 'D' vector. Represents the Cholesky of C^{-1} .
nID	N x k matrix of neighbor indices.

Value

A list with two components: (1) an N x 2 array containing the same spatial coordinates, ordered by MMD, and (2) the same thing, but with any NA values removed.

calculateAD_ns Calculate A and D matrices for the NNGP approximation

Description

calculateAD_ns calculates A and D matrices (the Cholesky of the precision matrix) needed for the NNGP approximation.

Usage

calculateAD_ns(dist1_3d, dist2_3d, dist12_3d, Sigma11, Sigma22, Sigma12, log_sigma_vec, log_tau_vec, nID, N, k, nu, d)

dist1_3d	N x (k+1) x (k+1) array of distances in the x-coordinate direction.
dist2_3d	N x (k+1) x (k+1) array of distances in the y-coordinate direction.
dist12_3d	N x (k+1) x (k+1) array of cross-distances.
Sigma11	N-vector; 1-1 element of the Sigma() process.
Sigma22	N-vector; 2-2 element of the Sigma() process.
Sigma12	N-vector; 1-2 element of the Sigma() process.
log_sigma_vec	N-vector; process standard deviation values.
log_tau_vec	N-vector; nugget standard deviation values.
nID	N x k matrix of neighbor indices.
Ν	Scalar; number of data measurements.
k	Scalar; number of nearest neighbors.
nu	Scalar; Matern smoothness parameter.
d	Scalar; dimension of the spatial domain.

Value

A N x (k+1) matrix; the first k columns are the 'A' matrix, and the last column is the 'D' vector.

calculateU_ns Calculate the (sparse) matrix U

Description

calculateU_ns calculates the (sparse) matrix U (i.e., the Cholesky of the inverse covariance matrix) using a nonstationary covariance function. The output only contains non-zero values and is stored as three vectors: (1) the row indices, (2) the column indices, and (3) the non-zero values. NOTE: this code assumes the all inputs correspond to the ORDERED locations.

Usage

```
calculateU_ns(
  dist1_3d,
  dist2_3d,
  dist12_3d,
  Sigmal1,
  Sigma22,
  Sigma12,
  log_sigma_vec,
  log_tau_vec,
  nu,
  nID,
  cond_on_y,
  Ν,
  k,
 d.
 M = 0
)
```

dist1_3d	N x (k+1) x (k+1) array of distances in the x-coordinate direction.
dist2_3d	N x (k+1) x (k+1) array of distances in the y-coordinate direction.
dist12_3d	N x (k+1) x (k+1) array of cross-distances.
Sigma11	N-vector; 1-1 element of the Sigma() process.
Sigma22	N-vector; 2-2 element of the Sigma() process.
Sigma12	N-vector; 1-2 element of the Sigma() process.
log_sigma_vec	N-vector; process standard deviation values.
log_tau_vec	N-vector; nugget standard deviation values.
nu	Scalar; Matern smoothness parameter.

conditionLatentObs

nID	N x k matrix of (ordered) neighbor indices.
cond_on_y	A matrix indicating whether the conditioning set for each (ordered) location is on the latent process $(y, 1)$ or the observed values $(z, 0)$. Calculated in sgvSetup.
Ν	Scalar; number of data measurements.
k	Scalar; number of nearest neighbors.
d	Scalar; dimension of the spatial domain.
М	Scalar; number of prediction sites.

Value

Returns a sparse matrix representation of the Cholesky of the precision matrix for a fixed set of covariance parameters.

conditionLatentObs Assign conditioning sets for the SGV approximation

Description

conditionLatentObs assigns $q_y(i)$ vs $q_z(i)$ following Section 5.1 in Katzfuss and Guinness (2018). This function only needs to be run once per SGV analysis.

Usage

conditionLatentObs(nID, coords_ord, N)

Arguments

nID	N x k matrix of neighbor indices.
coords_ord	N x 2 matrix of locations.
Ν	Scalar; number of locations (observed only!).

Value

A matrix indicating whether the conditioning set for each location is on the latent process (y, 1) or the observed values (z, 0).

determineNeighbors

Description

determineNeighbors returns an N x k matrix of the nearest neighbors for spatial locations coords, with the ith row giving indices of the k nearest neighbors to the ith location, which are selected from among the 1,...(i-1) other spatial locations. The first row is -1's, since the first location has no neighbors. The i=2 through i=(k+1) rows each necessarily contain 1:i.

Usage

```
determineNeighbors(coords, k)
```

Arguments

coords	N x 2 array of N 2-dimensional (x,y) spatial coordinates.
k	Scalar; number of neighbors

Value

An N x k matrix of nearest neighbor indices

Examples

```
coords <- cbind(runif(100), runif(100))
determineNeighbors(coords, 20)</pre>
```

dmnorm_nngp

Function for the evaluating the NNGP approximate density.

Description

dmnorm_nngp (and rmnorm_nngp) calculate the approximate NNGP likelihood for a fixed set of parameters (i.e., A and D matrices). Finally, the distributions must be registered within nimble.

Usage

dmnorm_nngp(x, mean, AD, nID, N, k, log)

dmnorm_sgv

Arguments

x	N-vector of data.
mean	N-vector with current values of the mean
AD	N x (k +1) matrix; the first k columns are the 'A' matrix, and the last column is the 'D' vector.
nID	N x k matrix of neighbor indices.
Ν	Scalar; number of data measurements.
k	Scalar; number of nearest neighbors.
log	Scalar; should the density be on the log scale (1) or not (0) .

Value

The NNGP approximate density.

dmnorm_sgv

Function for the evaluating the SGV approximate density.

Description

dmnorm_sgv (and rmnorm_sgv) calculate the approximate SGV likelihood for a fixed set of parameters (i.e., the U matrix). Finally, the distributions must be registered within nimble.

Usage

dmnorm_sgv(x, mean, U, N, k, log = 1)

Arguments

x	Vector of measurements
mean	Vector of mean values
U	Matrix of size N x 3; representation of a sparse N x N Cholesky of the precision matrix. The first two columns contain row and column indices, respectively, and the last column is the nonzero elements of the matrix.
Ν	Number of measurements in x
k	Number of neighbors for the SGV approximation.
log	Logical; should the density be evaluated on the log scale.

Value

Returns the SGV approximation to the Gaussian likelihood.

inverseEigen

Description

inverseEigen calculates the inverse eigendecomposition – in other words, the covariance elements based on the eigenvalues and vectors. For a 2x2 anisotropy (covariance) matrix, we parameterize the three unique values in terms of the two log eigenvalues and a rotation parameter on the rescaled logit. The function is coded as a nimbleFunction (see the nimble package) but can also be used as a regular R function.

Usage

```
inverseEigen(eigen_comp1, eigen_comp2, eigen_comp3, which_Sigma)
```

Arguments

eigen_comp1	N-vector; contains values of the log of the first anisotropy eigenvalue for a set of locations.
eigen_comp2	N-vector; contains values of the log of the second anisotropy eigenvalue for a set of locations.
eigen_comp3	N-vector; contains values of the rescaled logit of the anisotropy rotation for a set of locations.
which_Sigma	Scalar; one of (1,2,3), corresponding to which covariance component should be calculated (Sigma11, Sigma22, or Sigma12, respectively).

Value

A vector of anisotropy values (Sigma11, Sigma22, or Sigma12; depends on which_Sigma) for the corresponding set of locations.

Examples

```
# Generate some eigendecomposition elements (all three are real-valued)
eigen_comp1 <- rnorm(10)
eigen_comp2 <- rnorm(10)
eigen_comp3 <- rnorm(10)
inverseEigen( eigen_comp1, eigen_comp2, eigen_comp3, 2) # Return the Sigma22 values</pre>
```

matern_corr

Description

matern_corr calculates a stationary Matern correlation matrix for a fixed set of locations, based on a range and smoothness parameter. This function is primarily used for the "npGP" and "approxGP" models. The function is coded as a nimbleFunction (see the nimble package) but can also be used as a regular R function.

Usage

matern_corr(dist, rho, nu)

Arguments

dist	N x N matrix; contains values of pairwise Euclidean distances in the x-y plane.
rho	Scalar; "range" parameter used to rescale distances
nu	Scalar; Matern smoothness parameter. $nu = 0.5$ corresponds to the Exponential correlation; $nu = Inf$ corresponds to the Gaussian correlation function.

Value

A correlation matrix for a fixed set of stations and fixed parameter values.

Examples

```
# Generate some coordinates
coords <- cbind(runif(100),runif(100))
nu <- 2
# Calculate distances -- can use nsDist to calculate Euclidean distances
dist_list <- nsDist(coords, isotropic = TRUE)
# Calculate the correlation matrix
corMat <- matern_corr(sqrt(dist_list$dist1_sq), 1, nu)</pre>
```

nimble_sparse_chol nimble_sparse_chol

Description

nimble_sparse_chol

Usage

nimble_sparse_chol(i, j, x, n)

Arguments

i	Vector of row indices.
j	Vector of column indices.
х	Vector of values in the matrix.
n	Length of the vector

nimble_sparse_crossprod

nimble_sparse_crossprod

Description

nimble_sparse_crossprod

Usage

```
nimble_sparse_crossprod(i, j, x, z, n, subset, transp)
```

Arguments

i	Vector of row indices.
j	Vector of column indices.
х	Vector of values in the matrix.
Z	Vector to calculate the cross-product with.
n	Length of the vector
subset	Optional vector of rows to include in the calculation.
transp	Optional indicator of using the transpose

nimble_sparse_solve nimble_sparse_solve

Description

nimble_sparse_solve

Usage

nimble_sparse_solve(i, j, x, z)

i	Vector of row indices.
j	Vector of column indices.
х	Vector of values in the matrix.
z	Vector to calculate the cross-product with.

nimble_sparse_tcrossprod

nimble_sparse_tcrossprod

Description

nimble_sparse_tcrossprod

Usage

nimble_sparse_tcrossprod(i, j, x, subset)

Arguments

i	Vector of row indices.
j	Vector of column indices.
x	Vector of values in the matrix.
subset	Optional vector of rows to include in the calculation.

nsCorr

Calculate a nonstationary Matern correlation matrix

Description

nsCorr calculates a nonstationary correlation matrix for a fixed set of locations, based on vectors of the unique anisotropy parameters for each station. Since the correlation function uses a spatially-varying Mahalanobis distance, this function requires coordinate- specific distance matrices (see below). The function is coded as a nimbleFunction (see the nimble package) but can also be used as a regular R function.

Usage

```
nsCorr(dist1_sq, dist2_sq, dist12, Sigma11, Sigma22, Sigma12, nu, d)
```

dist1_sq	N x N matrix; contains values of pairwise squared distances in the x-coordinate.
dist2_sq	N x N matrix; contains values of pairwise squared distances in the y-coordinate.
dist12	N x N matrix; contains values of pairwise signed cross- distances between the x- and y-coordinates. The sign of each element is important; see nsDist function for the details of this calculation. in the x-coordinate.
Sigma11	Vector of length N; contains the 1-1 element of the anisotropy process for each station.

Sigma22	Vector of length N; contains the 2-2 element of the anisotropy process for each station.
Sigma12	Vector of length N; contains the 1-2 element of the anisotropy process for each station.
nu	Scalar; Matern smoothness parameter. nu = 0.5 corresponds to the Exponential correlation; nu = Inf corresponds to the Gaussian correlation function.
d	Scalar; dimension of the spatial coordinates.

Value

A correlation matrix for a fixed set of stations and fixed parameter values.

Examples

nsCrosscorr

Calculate a nonstationary Matern cross-correlation matrix

Description

nsCrosscorr calculates a nonstationary cross-correlation matrix between two fixed sets of locations (a prediction set with M locations, and the observed set with N locations), based on vectors of the unique anisotropy parameters for each station. Since the correlation function uses a spatially-varying Mahalanobis distance, this function requires coordinate- specific distance matrices (see below). The function is coded as a nimbleFunction (see the nimble package) but can also be used as a regular R function.

Usage

```
nsCrosscorr(
Xdist1_sq,
Xdist2_sq,
Xdist12,
Sigma11,
Sigma22,
```

nsCrosscorr

```
Sigma12,
PSigma11,
PSigma22,
PSigma12,
nu,
d
```

Arguments

)

Xdist1_sq	M x N matrix; contains values of pairwise squared cross-distances in the x-coordinate.
Xdist2_sq	M x N matrix; contains values of pairwise squared cross-distances in the y-coordinate.
Xdist12	M x N matrix; contains values of pairwise signed cross/cross- distances between the x- and y-coordinates. The sign of each element is important; see nsDist function for the details of this calculation. in the x-coordinate.
Sigma11	Vector of length N; contains the 1-1 element of the anisotropy process for each observed location.
Sigma22	Vector of length N; contains the 2-2 element of the anisotropy process for each observed location.
Sigma12	Vector of length N; contains the 1-2 element of the anisotropy process for each observed location.
PSigma11	Vector of length N; contains the 1-1 element of the anisotropy process for each prediction location.
PSigma22	Vector of length N; contains the 2-2 element of the anisotropy process for each prediction location.
PSigma12	Vector of length N; contains the 1-2 element of the anisotropy process for each prediction location.
nu	Scalar; Matern smoothness parameter. nu = 0.5 corresponds to the Exponential correlation; nu = Inf corresponds to the Gaussian correlation function.
d	Scalar; dimension of the spatial domain.

Value

A M x N cross-correlation matrix for two fixed sets of stations and fixed parameter values.

Examples

```
# Generate some coordinates and parameters
coords <- cbind(runif(100),runif(100))
Sigma11 <- rep(1, 100) # Identity anisotropy process
Sigma22 <- rep(1, 100)
Sigma12 <- rep(0, 100)
Pcoords <- cbind(runif(200),runif(200))
PSigma11 <- rep(1, 200) # Identity anisotropy process
PSigma22 <- rep(1, 200)</pre>
```

```
PSigma12 <- rep(0, 200)
nu <- 2
# Calculate distances
Xdist_list <- nsCrossdist(coords, Pcoords)
# Calculate the correlation matrix
XcorMat <- nsCrosscorr(Xdist_list$dist1_sq, Xdist_list$dist2_sq, Xdist_list$dist12,
    Sigma11, Sigma22, Sigma12, PSigma11, PSigma22, PSigma12, nu, ncol(coords))</pre>
```

nsCrossdist

```
Calculate coordinate-specific cross-distance matrices
```

Description

nsCrossdist calculates coordinate-specific cross distances in x, y, and x-y for use in the nonstationary cross-correlation calculation. This function is useful for calculating posterior predictions.

Usage

```
nsCrossdist(coords, Pcoords, scale_factor = NULL, isotropic = FALSE)
```

Arguments

coords	N x 2 matrix; contains x-y coordinates of station (observed) locations.
Pcoords	M x 2 matrix; contains x-y coordinates of prediction locations.
scale_factor	Scalar; optional argument for re-scaling the distances.
isotropic	Logical; indicates whether distances should be calculated using Euclidean dis- tance (isotropic = TRUE) or using the anisotropic formulation (isotropic = FALSE).

Value

A list of distances matrices, with the following components:

dist1_sq	M x N matrix; contains values of pairwise squared cross- distances in the x-coordinate.
dist2_sq	M x N matrix; contains values of pairwise squared cross- distances in the y-coordinate.
dist12	M x N matrix; contains values of pairwise signed cross- distances between the x- and y-coordinates.
scale_factor	Value of the scale factor used to rescale distances.

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nsCrossdist3d

Examples

```
# Generate some coordinates
coords <- cbind(runif(100),runif(100))
Pcoords <- cbind(runif(200),runif(200))
# Calculate distances
Xdist_list <- nsCrossdist(coords, Pcoords)</pre>
```

nsCrossdist3d

Calculate coordinate-specific cross-distance matrices, only for nearest neighbors and store in an array

Description

nsCrossdist3d generates and returns new 3-dimensional arrays containing the former dist1_sq, dist2_s1, and dist12 matrices, but only as needed for the k nearest-neighbors of each location. these 3D matrices (dist1_3d, dist2_3d, and dist12_3d) are used in the new implementation of calculateAD_ns().

Usage

```
nsCrossdist3d(
  coords,
  predCoords,
  P_nID,
  scale_factor = NULL,
  isotropic = FALSE
)
```

Arguments

coords	N x d matrix; contains the x-y coordinates of stations.
predCoords	M x d matrix
P_nID	N x k matrix; contains indices of nearest neighbors.
scale_factor	Scalar; optional argument for re-scaling the distances.
isotropic	Logical; indicates whether distances should be calculated separately for each coordinate dimension (FALSE) or simultaneously for all coordinate dimensions (TRUE). isotropic = FALSE can only be used for two-dimensional coordinate systems.

Value

Arrays with nearest neighbor distances in each coordinate direction. When the spatial dimension d > 2, dist1_3d contains squared Euclidean distances, and dist2_3d and dist12_3d are empty.

Examples

```
# Generate some coordinates and neighbors
coords <- cbind(runif(100),runif(100))
predCoords <- cbind(runif(200),runif(200))
P_nID <- FNN::get.knnx(coords, predCoords, k = 10)$nn.index # Prediction NN
# Calculate distances
Pdist <- nsCrossdist3d(coords, predCoords, P_nID)</pre>
```

nsDist

```
Calculate coordinate-specific distance matrices
```

Description

nsDist calculates x, y, and x-y distances for use in the nonstationary correlation calculation. The sign of the cross-distance is important. The function contains an optional argument for re-scaling the distances such that the coordinates lie in a square.

Usage

```
nsDist(coords, scale_factor = NULL, isotropic = FALSE)
```

Arguments

coords	N x 2 matrix; contains the x-y coordinates of stations
scale_factor	Scalar; optional argument for re-scaling the distances.
isotropic	Logical; indicates whether distances should be calculated separately for each coordinate dimension (FALSE) or simultaneously for all coordinate dimensions (TRUE). isotropic = TRUE can only be used for two-dimensional coordinate systems.

Value

A list of distances matrices, with the following components:

dist1_sq	N x N matrix; contains values of pairwise squared distances in the x-coordinate.
dist2_sq	N x N matrix; contains values of pairwise squared distances in the y-coordinate.
dist12	N x N matrix; contains values of pairwise signed cross- distances between the x- and y-coordinates.
scale_factor	Value of the scale factor used to rescale distances.

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nsDist3d

Examples

```
# Generate some coordinates
coords <- cbind(runif(100),runif(100))
# Calculate distances
dist_list <- nsDist(coords)
# Use nsDist to calculate Euclidean distances
dist_Euclidean <- sqrt(nsDist(coords, isotropic = TRUE)$dist1_sq)</pre>
```

nsDist3d

Calculate coordinate-specific distance matrices, only for nearest neighbors and store in an array

Description

nsDist3d generates and returns new 3-dimensional arrays containing the former dist1_sq, dist2_sq, and dist12 matrices, but only as needed for the k nearest-neighbors of each location. these 3D matrices (dist1_3d, dist2_3d, and dist12_3d) are used in the new implementation of calculateAD_ns().

Usage

nsDist3d(coords, nID, scale_factor = NULL, isotropic = FALSE)

Arguments

coords	N x 2 matrix; contains the x-y coordinates of stations.
nID	N x k matrix; contains indices of nearest neighbors.
scale_factor	Scalar; optional argument for re-scaling the distances.
isotropic	Logical; indicates whether distances should be calculated separately for each coordinate dimension (FALSE) or simultaneously for all coordinate dimensions (TRUE). isotropic = TRUE can only be used for two-dimensional coordinate systems.

Value

Arrays with nearest neighbor distances in each coordinate direction.

Examples

```
# Generate some coordinates and neighbors
coords <- cbind(runif(100),runif(100))
nID <- determineNeighbors(coords, 10)
# Calculate distances
nsDist3d(coords, nID)
```

nsgpModel

Description

This function sets up and compiles a nimble model for a general nonstationary Gaussian process.

Usage

```
nsgpModel(
  tau_model = "constant",
  sigma_model = "constant",
  Sigma_model = "constant",
  mu_model = "constant",
  likelihood = "fullGP",
  coords,
  data,
  constants = list(),
  monitorAllSampledNodes = TRUE,
  ...
)
```

tau_model	Character; specifies the model to be used for the log(tau) process. Options are "constant" (spatially-constant), "logLinReg" (log-linear regression), and "approxGP" (approximation to a Gaussian process).
sigma_model	Character; specifies the model to be used for the log(sigma) process. See tau_model for options.
Sigma_model	Character; specifies the model to be used for the Sigma anisotropy process. Op- tions are "constant" (spatially-constant), "constantIso" (spatially-constant and isotropic), "covReg" (covariance regression), "compReg" (componentwise regression), "compRegIso" (isotropic componentwise regression), "npApproxGP" (nonparameteric regression via an approximation to a stationary Gaussian pro- cess), and "npApproxGPIso" (isotropic nonparameteric regression via an ap- proximation to a stationary Gaussian process)
mu_model	Character; specifies the model to be used for the mu mean process. Options are "constant" (spatially-constant), "linReg" (linear regression), and "zero" (a fixed zero-mean).
likelihood	Character; specifies the likelihood model. Options are "fullGP" (the exact Gaussian process likelihood), "NNGP" (the nearest-neighbor GP for the response approximate likelihood), and "SGV" (the sparse general Vecchia approximate likelihood).
coords	N x d matrix of spatial coordinates.
data	N-vector; observed vector of the spatial process of interest

nsgpPredict

constants	A list of constants required to build the model; depends on the specific parameter process models chosen.	
monitorAllSampledNodes		
	Logical; indicates whether all sampled nodes should be stored (TRUE) or not (FALSE).	
	Additional arguments can be passed to the function; for example, as an alterna- tive to the constants list, items can be passed directly via this argument.	

Value

A nimbleCode object.

Examples

```
# Generate some data: stationary/isotropic
N <- 100
coords <- matrix(runif(2*N), ncol = 2)</pre>
alpha_vec <- rep(log(sqrt(1)), N) # Log process SD</pre>
delta_vec <- rep(log(sqrt(0.05)), N) # Log nugget SD</pre>
Sigma11_vec <- rep(0.4, N) # Kernel matrix element 1,1</pre>
Sigma22_vec <- rep(0.4, N) # Kernel matrix element 2,2
Sigma12_vec <- rep(0, N) # Kernel matrix element 1,2</pre>
mu_vec <- rep(0, N) # Mean</pre>
nu <- 0.5 # Smoothness</pre>
dist_list <- nsDist(coords)</pre>
Cor_mat <- nsCorr( dist1_sq = dist_list$dist1_sq, dist2_sq = dist_list$dist2_sq,</pre>
                    dist12 = dist_list$dist12, Sigma11 = Sigma11_vec,
                    Sigma22 = Sigma22_vec, Sigma12 = Sigma12_vec, nu = nu )
Cov_mat <- diag(exp(alpha_vec)) %*% Cor_mat %*% diag(exp(alpha_vec))</pre>
D_mat <- diag(exp(delta_vec)^2)</pre>
set.seed(110)
data <- as.numeric(mu_vec + t(chol(Cov_mat + D_mat)) %*% rnorm(N))</pre>
# Set up constants
constants <- list( nu = 0.5, Sigma_HP1 = 2 )</pre>
# Defaults: tau_model = "constant", sigma_model = "constant", mu_model = "constant",
# and Sigma_model = "constant"
Rmodel <- nsgpModel(likelihood = "fullGP", constants = constants, coords = coords, data = data)
```

nsgpPredict

Posterior prediction for the NSGP

Description

nsgpPredict conducts posterior prediction for MCMC samples generated using nimble and nsgp-Model.

Usage

```
nsgpPredict(
  model,
  samples,
  coords.predict,
  predict.process = TRUE,
  constants,
  seed = 0,
  ...
)
```

Arguments

model	A NSGP nimble object; the output of nsgpModel.
samples	A matrix of J rows, each is an MCMC sample of the parameters corresponding to the specification in nsgpModel.
coords.predict	M x d matrix of prediction coordinates.
predict.process	6
	Logical; determines whether the prediction corresponds to the $y(\cdot)$ process (TRUE) or $z(\cdot)$ (FALSE; this would likely only be used for, e.g., cross-validation).
constants	An optional list of contants to use for prediction; alternatively, additional arguments can be passed to the function via the argument.
seed	An optional random seed argument for reproducibility.
	Additional arguments can be passed to the function; for example, as an alterna- tive to the constants list, items can be passed directly via this argument.

Value

The output of the function is a list with two elements: obs, a matrix of J posterior predictive samples for the N observed locations (only for likelihood = "SGV", which produces predictions for the observed locations by default; this element is NULL otherwise); and pred, a corresponding matrix of posterior predictive samples for the prediction locations. Ordering and neighbor selection for the prediction coordinates in the SGV likelihood are conducted internally, as with nsgpModel.

Examples

```
# Generate some data: stationary/isotropic
N <- 100
coords <- matrix(runif(2*N), ncol = 2)
alpha_vec <- rep(log(sqrt(1)), N) # Log process SD
delta_vec <- rep(log(sqrt(0.05)), N) # Log nugget SD
Sigma11_vec <- rep(0.4, N) # Kernel matrix element 1,1
Sigma22_vec <- rep(0.4, N) # Kernel matrix element 2,2
Sigma12_vec <- rep(0, N) # Kernel matrix element 1,2
mu_vec <- rep(0, N) # Mean
nu <- 0.5 # Smoothness
dist_list <- nsDist(coords)
Cor_mat <- nsCorr( dist1_sq = dist_list$dist1_sq, dist2_sq = dist_list$dist2_sq,</pre>
```

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```
dist12 = dist_list$dist12, Sigma11 = Sigma11_vec,
                    Sigma22 = Sigma22_vec, Sigma12 = Sigma12_vec, nu = nu )
Cov_mat <- diag(exp(alpha_vec)) %*% Cor_mat %*% diag(exp(alpha_vec))</pre>
D_mat <- diag(exp(delta_vec)^2)</pre>
set.seed(110)
data <- as.numeric(mu_vec + t(chol(Cov_mat + D_mat)) %*% rnorm(N))</pre>
# Set up constants
constants <- list( nu = 0.5, Sigma_HP1 = 2 )</pre>
# Defaults: tau_model = "constant", sigma_model = "constant", mu_model = "constant",
# and Sigma_model = "constant"
Rmodel <- nsgpModel(likelihood = "fullGP", constants = constants, coords = coords, data = data)
conf <- configureMCMC(Rmodel)</pre>
Rmcmc <- buildMCMC(conf)</pre>
Cmodel <- compileNimble(Rmodel)</pre>
Cmcmc <- compileNimble(Rmcmc, project = Rmodel)</pre>
samples <- runMCMC(Cmcmc, niter = 200, nburnin = 100)</pre>
# Prediction
predCoords <- as.matrix(expand.grid(seq(0,1,1=10),seq(0,1,1=10)))</pre>
postpred <- nsgpPredict( model = Rmodel, samples = samples, coords.predict = predCoords )</pre>
```

orderCoordinatesMMD Order coordinates according to a maximum-minimum distance criterion.

Description

orderCoordinatesMMD orders an array of (x,y) spatial coordinates according to the "maximum minimum distance" (MMD), as described in Guinness, 2018. (Points are selected to maximize their minimum distance to already- selected points).

Usage

orderCoordinatesMMD(coords, exact = FALSE)

Arguments

coords	N x 2 array of N 2-dimensional (x,y) spatial coordinates.
exact	Logical; FALSE uses a fast approximation to MMD ordering (and is almost al-
	ways recommended), while TRUE uses exact MMD ordering but is infeasible for
	large number of locations.

Value

A list of distances matrices, with the following components:

orderedCoords N x 2 matrix; contains the ordered spatial coordinates as coords. orderedIndicesNoNA

N-vector; contains the ordered indices with any NA values removed.

Examples

```
coords <- cbind(runif(100), runif(100))
orderCoordinatesMMD(coords)</pre>
```

rmnorm_nngp

Function for the evaluating the NNGP approximate density.

Description

dmnorm_nngp (and rmnorm_nngp) calculate the approximate NNGP likelihood for a fixed set of parameters (i.e., A and D matrices). Finally, the distributions must be registered within nimble.

Usage

rmnorm_nngp(n, mean, AD, nID, N, k)

Arguments

n	N-vector of data.
mean	N-vector with current values of the mean
AD	N x (k +1) matrix; the first k columns are the 'A' matrix, and the last column is the 'D' vector.
nID	N x k matrix of neighbor indices.
Ν	Scalar; number of data measurements.
k	Scalar; number of nearest neighbors.

Value

The NNGP approximate density.

rmnorm_sg∨	Function for the evaluating the SGV a	approximate density.
------------	---------------------------------------	----------------------

Description

dmnorm_sgv (and rmnorm_sgv) calculate the approximate SGV likelihood for a fixed set of parameters (i.e., the U matrix). Finally, the distributions must be registered within nimble.

Usage

rmnorm_sgv(n, mean, U, N, k)

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R_sparse_chol

Arguments

n	Vector of measurements
mean	Vector of mean values
U	Matrix of size N x 3; representation of a sparse N x N Cholesky of the precision matrix. The first two columns contain row and column indices, respectively, and the last column is the nonzero elements of the matrix.
Ν	Number of measurements in x
k	Number of neighbors for the SGV approximation.

Value

Not applicable.

R_sparse_chol R_sparse_chol

Description

R_sparse_chol

Usage

R_sparse_chol(i, j, x, n)

Arguments

i	Vector of row indices.
j	Vector of column indices.
х	Vector of values in the matrix.
n	Length of the vector

R_sparse_crossprod nimble_sparse_crossprod

Description

nimble_sparse_crossprod

Usage

```
R_sparse_crossprod(i, j, x, z, n, subset = -1, transp = 1)
```

Arguments

i	Vector of row indices.
j	Vector of column indices.
х	Vector of values in the matrix.
Z	Vector to calculate the cross-product with.
n	Length of the vector
subset	Optional vector of rows to include in the calculation.
transp	Optional indicator of using the transpose

R_sparse_solve nimble_sparse_solve

Description

nimble_sparse_solve

Usage

R_sparse_solve(i, j, x, z)

Arguments

i	Vector of row indices.
j	Vector of column indices.
х	Vector of values in the matrix.
z	Vector to calculate the cross-product with.

R_sparse_tcrossprod nimble_sparse_tcrossprod

Description

nimble_sparse_tcrossprod

Usage

R_sparse_tcrossprod(i, j, x, subset = -1)

i	Vector of row indices.
j	Vector of column indices.
х	Vector of values in the matrix.
subset	Optional vector of rows to include in the calculation.

Description

sgvSetup is a wrapper function that sets up the SGV approximation. Three objects are required: (1) ordering the locations, (2) identify nearest neighbors, and (3) determine the conditioning set. This function only needs to be run once per SGV analysis.

Usage

```
sgvSetup(
  coords,
  coords_pred = NULL,
  k = 15,
  seed = NULL,
  pred.seed = NULL,
  order_coords = TRUE
)
```

Arguments

coords	Matrix of observed locations.
coords_pred	Optional matrix of prediction locations.
k	Number of neighbors.
seed	Setting the seed for reproducibility of the observed location ordering
pred.seed	Setting the seed for reproducibility of the prediction ordering.
order_coords	Logical; should the coordinates be ordered.

Value

A list with the following components:

ord	A vector of ordering position for the observed locations.
ord_pred	A vector of ordering position for the prediction locations (if coords_pred is provided).
ord_all	A concatenated vector of ord and ord_pred.
coords_ord	A matrix of ordered locations (observed and prediction), included for convenience.
nID_ord	A matrix of (ordered) neighbor indices.
condition_on_y_ord	
	A matrix indicating whether the conditioning set for each (ordered) location is on the latent process $(y, 1)$ or the observed values $(z, 0)$.

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